

Learning Target: Today you will be able to SOLVE ONE-STEP EQUATIONS IN ONE VARIABLE

Question/Main Ideas:	Notes:	
Definition: Equivalent Equations	Equations that have the same solution(s).	
Property: Addition and Subtraction Properties of Equality	Addition Property of Equality - For any real number $a, b,$ and $c.$ If... $a=b$ then $a+c=b+c$	Subtraction Property of Equality - For any real number $a, b,$ and c If... $a=b$ then $a-c=b-c$
Definition: Isolate	Get the variable "alone" with a coefficient of one.	
Definition: Inverse Operation	Undoes another operation. Addition \leftrightarrow Subtraction; Multiplication \leftrightarrow Division	
Example 1: Solving One-Step Equations using Adding and Subtracting	Solve each equation. Justify each step. <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>a. $x + 13 = 27$</p> $\frac{-13 \quad -13}{x = 14}$ <p>Sub. Prop. of Equal.</p> </div> <div style="text-align: center;"> <p>b. $-7 = x - 3$</p> $\frac{+3 \quad +3}{-4 = x}$ <p>Add. Prop. of Equal.</p> </div> </div>	
Now It's Your Turn	Solve each equation. Justify each step. <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>a. $y + 2 = -6$</p> $\frac{-2 \quad -2}{y = -8}$ <p>Sub. Prop. of Equal.</p> </div> <div style="text-align: center;"> <p>b. $\frac{1}{2} = x - \frac{3}{2}$</p> $\frac{+\frac{3}{2} \quad +\frac{3}{2}}{\frac{4}{2} = x}$ <p>Add Prop. of Equal.</p> <p>$x = 2$</p> </div> </div>	
Property: Multiplication and Division Properties of Equality	Multiplication Property of Equality - For any real number $a, b,$ and $c.$ If... $a=b$ then $a \cdot c = b \cdot c$	Division Property of Equality - For any real number $a, b,$ and $c.$ If... $a=b$ then $\frac{a}{c} = \frac{b}{c}$

Example 2: Solving One-Step Equations using Multiplying and Dividing

Solve each equation. Justify each step.

a. $\frac{4x}{4} = \frac{6.4}{4}$ Div. Prop. of Equal.
 $x = 1.6$

b. $\frac{x}{4} = -20 \cdot 4$ Mult. Prop. of Equal.
 $x = -80$

Now It's Your Turn

Solve each equation. Justify each step.

a. $10 = \frac{15x}{15}$ Div. Prop. of Equal.
 $\frac{2}{3} = x$

b. $19 = \frac{x}{3} \cdot 3$ Mult. Prop. of Equal
 $57 = x$

Review: Dividing Fractions

Simplify the following.

$$\frac{3}{4} \div \frac{2}{3} = \frac{3}{4} \cdot \frac{3}{2} = \frac{6}{8} = \frac{3}{4}$$

Example 3: Solving Equations Using Reciprocals

Solve each equation. Justify each step.

$\frac{5}{4} \cdot \frac{4}{5}x = 28 \cdot \frac{5}{4}$ Mult. Prop. of Equal \rightarrow Dividing is the same as mult. by the reciprocal
 $x = 35$

Now It's Your Turn

Solve each equation. Justify each step.

$\frac{4}{3} \cdot 12 = \frac{3}{4}x \cdot \frac{4}{3}$ Mult. prop. of Equal.
 $16 = x$

Summary: _____

Learning Target: Today you will be able to SOLVE TWO-STEP EQUATIONS IN ONE VARIABLE

Question/Main Ideas:	Notes:
<p>Steps to Solving Two-Step Equations</p>	<p>Goal: <i>Isolate the variable</i></p> <hr/> <p><i>Add or subtract the constant term to eliminate it. Use inverse operations.</i></p> <hr/> <p><i>Multiply or divide to eliminate the coefficient. Use inverse operations.</i></p>
<p>Example 1: Solving a Two-Step Equation</p>	<p>Solve each equation.</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>a. $2x + 3 = 15$</p> $\begin{array}{r} -3 \quad -3 \\ \hline 2x = 12 \\ \frac{2x}{2} = \frac{12}{2} \\ x = 6 \end{array}$ </div> <div style="text-align: center;"> <p>b. $\frac{1}{2}x + 5 = 18$</p> $\begin{array}{r} -5 \quad -5 \\ \hline 2 \cdot \frac{1}{2}x = 13 \cdot 2 \\ x = 26 \end{array}$ </div> </div>
<p>Now It's Your Turn</p>	<p>Solve each equation.</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>a. $5 = \frac{x}{2} - 3$</p> $\begin{array}{r} +3 \quad +3 \\ \hline 2 \cdot 8 = \frac{x}{2} \cdot 2 \\ 16 = x \end{array}$ </div> <div style="text-align: center;"> <p>b. $-5 + 4x = 11$</p> $\begin{array}{r} +5 \quad +5 \\ \hline \frac{4x}{4} = \frac{16}{4} \\ x = 4 \end{array}$ </div> </div>

Summary: _____

Learning Target: Today you will be able to SOLVE TWO-STEP EQUATIONS USING FRACTION BUSTERS

Question/Main Ideas:	Notes:
<p>Fraction Busters</p>	<p>Multiply the entire equation by $\frac{2}{3} \cdot 6 = \frac{12}{3} = 4$ the common denominator</p>
<p>Concept: The Benefits of Fraction Busters</p>	<p>Solve each equation.</p> <p>a. $\frac{2}{5}x + \frac{3}{5} = \frac{1}{3} \quad \frac{5}{15}$</p> $\begin{array}{r} \frac{2}{5}x + \frac{3}{5} = \frac{1}{3} \\ -\frac{3}{5} \quad -\frac{3}{5} \quad -\frac{9}{15} \\ \hline \frac{2}{5}x = -\frac{4}{15} \end{array}$ $\frac{5}{2} \cdot \frac{2}{5}x = -\frac{4}{15} \cdot \frac{5}{2}$ $x = -\frac{20}{30} = -\frac{2}{3}$ <p>b. $\left(\frac{2}{5}x + \frac{3}{5} = \frac{1}{3}\right) 15$</p> $\begin{array}{r} 6x + 9 = 5 \\ -9 \quad -9 \\ \hline 6x = 4 \\ \frac{6x}{6} = \frac{4}{6} \quad x = \frac{2}{3} \end{array}$
<p>Example 1: Using Fraction Busters</p>	<p>Solve each equation.</p> <p>a. $\left(\frac{x-7}{3} = -12\right) 3$</p> $\begin{array}{r} x - 7 = -36 \\ +7 \quad +7 \\ \hline x = -29 \end{array}$ <p>b. $\left(\frac{x}{4} + 3 = 5\right) 4$</p> $\begin{array}{r} x + 12 = 20 \\ -12 \quad -12 \\ \hline x = 8 \end{array}$
<p>Now It's Your Turn</p>	<p>Solve each equation.</p> <p>a. $\left(6 = \frac{x-2}{4}\right) 4$</p> $\begin{array}{r} 24 = x - 2 \\ +2 \quad +2 \\ \hline 26 = x \end{array}$ <p>b. $\left(\frac{2}{3}x - 2 = \frac{5}{7}\right) 21$</p> $\begin{array}{r} 14x - 42 = 15 \\ +42 \quad +42 \\ \hline 14x = 57 \\ \frac{14x}{14} = \frac{57}{14} \quad x = 4.1 \end{array}$

Summary: _____

Learning Target: Today you will be able to SOLVE MULTI-STEP EQUATIONS USING EITHER DISTRIBUTIVE PROPERTY OR COMBINING LIKE TERMS

Question/Main Ideas:	Notes:
Key to Solving Multi-Step Equations	<p>Simplify First:</p> <ul style="list-style-type: none"> • Distributive Property • Combine Like terms
Example 1: Combining Like Terms	<p>Solve the following equation.</p> $5 = 5m - 23 + 2m$ $5 = 7m - 23$ $\begin{array}{r} +23 \\ \hline 28 = 7m \end{array}$ $\frac{28}{7} = \frac{7m}{7}$ $4 = m$
Now It's Your Turn	<p>Solve each equation.</p> <p>a. $11x - 8 - 6x = 22$</p> $5x - 8 = 22$ $\begin{array}{r} +8 \\ \hline 5x = 30 \end{array}$ $\frac{5x}{5} = \frac{30}{5}$ $x = 6$ <p>b. $-2x + 5 + 5x = 14$</p> $3x + 5 = 14$ $\begin{array}{r} -5 \\ \hline 3x = 9 \end{array}$ $\frac{3x}{3} = \frac{9}{3}$ $x = 3$
Example 2: Solving an Equations Using the Distributive Property	<p>Solve the following equation.</p> $-8(2x - 1) = 36$ $-16x + 8 = 36$ $\begin{array}{r} -8 \\ \hline -16x = 28 \end{array}$ $\frac{-16x}{-16} = \frac{28}{-16}$ $x = -1.75$

Now It's Your Turn

a. Solve $18 = 3(2x - 6)$.

$$\begin{array}{r} 18 = 6x - 18 \\ +18 \quad +18 \\ \hline 36 = 6x \\ \frac{36}{6} = \frac{6x}{6} \\ 6 = x \end{array}$$

b. Can you solve this equation by using the Division Property of Equality instead of the Distributive Property? Explain.

$$\begin{array}{r} 18 = 3(2x - 6) \\ \frac{18}{3} = \frac{3(2x - 6)}{3} \\ 6 = 2x - 6 \end{array} \leftarrow \begin{array}{l} \text{solve} \\ \text{this} \end{array}$$

Example 3: Solving an Equation that Contains Fractions

Solve $\frac{3x}{4} - \frac{x}{3} = 10$ using two different methods as described below.

a. Method 1: Using Like Terms

$$\begin{array}{r} \frac{3}{3} \cdot \frac{3x}{4} - \frac{x}{3} \cdot \frac{4}{4} = 10 \\ \frac{9x}{12} - \frac{4x}{12} = 10 \\ \frac{12}{5} \cdot \frac{5x}{12} = 10 \cdot \frac{12}{5} \\ x = 24 \end{array}$$

b. Method 2: Fraction Busters

$$\begin{array}{r} 12 \left(\frac{3x}{4} - \frac{x}{3} = 10 \right) \\ 9x - 4x = 120 \\ 5x = 120 \\ \frac{5x}{5} = \frac{120}{5} \\ x = 24 \end{array}$$

Now It's Your Turn

Solve each equation. Use a method of your choice.

$$\begin{array}{r} a. \left(\frac{5}{6}x + \frac{3}{4}x = 1 \right) 12 \\ 10x + 9x = 12 \\ 19x = 12 \\ x = \frac{12}{19} \end{array}$$

$$\begin{array}{r} b. \left(\frac{x}{5} - 3 + \frac{6x}{7} = 10 \right) 35 \\ 7x - 105 + 30x = 350 \\ 37x - 105 = 350 \\ \quad +105 +105 \\ \hline 37x = 245 \\ \frac{37x}{37} = \frac{245}{37} \\ x \approx 6.6 \end{array}$$

Example 4: Solving Equations that Contain Decimals

a. Solve $(3.5 - 0.02x = 1.24)$ 100

$$\begin{array}{r} 350 - 2x = 124 \\ -350 \quad -350 \\ \hline -2x = -226 \\ x = 113 \end{array}$$

b. Your Turn $(0.5x - 2.325 = 3.95)$ 1000

$$\begin{array}{r} 500x - 2325 = 3950 \\ \quad +2325 +2325 \\ \hline 500x = 6275 \\ \frac{500x}{500} = \frac{6275}{500} \\ x = 12.55 \end{array}$$

Summary:

Learning Target: Today you will be able to SOLVE MULTI-STEP EQUATIONS USING DISTRIBUTIVE PROPERTY AND COMBINING LIKE TERMS

Question/Main Ideas:	Notes:
Steps to Solving Multi-Step Equations	<p>Distributive Property</p> <p>Combine Like terms</p> <p>Isolate the variable</p>
Example 1: Solving Multi-Step Equations	<p>Solve each equation.</p> <p>a. $49 = 2(7x + 6) + 9$</p> $49 = 14x + 12 + 9$ $49 = 14x + 21$ $\begin{array}{r} -21 \\ \hline 28 = 14x \\ \frac{14}{14} \quad \frac{14}{14} \\ 2 = x \end{array}$ <p>b. $8(3x + 8) - 2x = 130$</p> $24x + 64 - 2x = 130$ $22x + 64 = 130$ $\begin{array}{r} -64 \\ \hline 22x = 66 \\ \frac{22}{22} \quad \frac{66}{22} \\ x = 3 \end{array}$
Now It's Your Turn	<p>Solve each equation.</p> <p>a. $12x - 2(x - 5) = 80$</p> $12x - 2x + 10 = 80$ $10x + 10 = 80$ $\begin{array}{r} -10 \\ \hline 10x = 70 \\ \frac{10}{10} \quad \frac{70}{10} \\ x = 7 \end{array}$ <p>b. $47 = 3(-2x + 4) + 11$</p> $47 = -6x + 12 + 11$ $47 = -6x + 23$ $\begin{array}{r} -23 \\ \hline 24 = -6x \\ \frac{24}{-6} \quad \frac{-6x}{-6} \\ -4 = x \end{array}$

Summary: _____

Learning Target: Today you will be able to SOLVE EQUATIONS WITH VARIABLES ON BOTH SIDES

Question/Main Ideas:	Notes:
Key Ideas	<p>Add or subtract the variable terms to move the variables to one side of the equation. Use inverse operations.</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> $\begin{array}{r} 3x + 5 = -8x + 11 \\ -3x \quad -3x \\ \hline 5 = -11x + 11 \end{array}$ </div> <div style="text-align: center;"> $\begin{array}{r} 3x + 5 = -8x + 11 \\ +8x \quad +8x \\ \hline 11x + 5 = 11 \end{array}$ </div> </div>
Example 1: Solving Equations with Variables on Both Sides	<p>Solve each equation.</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>a. $5x + 2 = 2x + 14$</p> $\begin{array}{r} 5x + 2 = 2x + 14 \\ -2x \quad -2x \\ \hline 3x + 2 = 14 \\ -2 \quad -2 \\ \hline 3x = 12 \\ \frac{3}{3} \quad \frac{12}{3} \\ x = 4 \end{array}$ </div> <div style="text-align: center;"> <p>b. $-6x - 7 = -4x + 3$</p> $\begin{array}{r} -6x - 7 = -4x + 3 \\ +6x \quad +6x \\ \hline -7 = 2x + 3 \\ -3 \quad -3 \\ \hline -10 = 2x \\ \frac{-10}{2} \quad \frac{2x}{2} \\ -5 = x \end{array}$ </div> </div>
Now It's Your Turn	<p>Solve each equation.</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>a. $7x + 2 = 4x - 10$</p> $\begin{array}{r} 7x + 2 = 4x - 10 \\ -4x \quad -4x \\ \hline 3x + 2 = -10 \\ -2 \quad -2 \\ \hline 3x = -12 \\ \frac{3x}{3} = \frac{-12}{3} \\ x = -4 \end{array}$ </div> <div style="text-align: center;"> <p>b. $3x - 10 = -2x + 15$</p> $\begin{array}{r} 3x - 10 = -2x + 15 \\ +2x \quad +2x \\ \hline 5x - 10 = 15 \\ +10 \quad +10 \\ \hline 5x = 25 \\ \frac{5x}{5} = \frac{25}{5} \\ x = 5 \end{array}$ </div> </div>

Example 2: Using an Equations with Variables on Both Sides

It takes a graphic designer 1.5 hours to make one page of a web site. Using new software, the designer could complete each page in 1.25 hours, but it takes 8 hours to learn the software. How many web pages would the designer have to make in order to save time using the new software?

$$\begin{array}{r}
 1.5x = 1.25x + 8 \\
 -1.25x \quad -1.25x \\
 \hline
 0.25x = 8 \\
 \cdot 25 \quad \cdot 25 \\
 \hline
 x = 32
 \end{array}$$

The designer would need to make more than 32 pages

Now It's Your Turn

An office manager spent \$650 on a new energy-saving copier that will reduce the monthly electric bill for the office from \$112 to \$88. In how many months will the copier pay for itself?

$$\begin{array}{r}
 112x = 88x + 650 \\
 -88x \quad -88x \\
 \hline
 24x = 650 \\
 x = 27.08
 \end{array}$$

28 months

Combining Like Terms vs. Variables on Both Sides

Solve $3x - 7 + 2x = 10$

$$\begin{array}{r}
 5x - 7 = 10 \\
 +7 \quad +7 \\
 \hline
 5x = 17 \\
 \frac{5x}{5} = \frac{17}{5} \\
 x = 3.4
 \end{array}$$

Solve $3x - 7 = 2x + 10$

$$\begin{array}{r}
 -2x \quad -2x \\
 \hline
 x - 7 = 10 \\
 +7 \quad +7 \\
 \hline
 x = 17
 \end{array}$$

Combining Like Terms Key Idea:

Same side of equation - do same operation

Variables on Both Sides Key Idea:

Opposite side of equation - use opposite operation.

Summary: _____

Learning Target: Today you will be able to SOLVE EQUATIONS WITH VARIABLES ON BOTH SIDES

Question/Main Ideas:	Notes:
Main Idea:	Simplify each side of the equation first like two separate problems.
Example 1: Solving Equations with Variables on Both Sides	<p>Solve each equation.</p> <p>a. $2(5x - 1) = 3(x + 11)$</p> $\begin{array}{r} 10x - 2 = 3x + 33 \\ -3x \quad -3x \\ \hline 7x - 2 = 33 \\ +2 \quad +2 \\ \hline 7x = 35 \\ x = 5 \end{array}$ <p>b. $7x - 5(x - 4) = 7(2x + 1)$</p> $\begin{array}{r} 7x - 5x + 20 = 14x + 7 \\ 2x + 20 = 14x + 7 \\ -2x \quad -2x \\ \hline 20 = 12x + 7 \\ -7 \quad -7 \\ \hline 13 = 12x \\ \frac{13}{12} = \frac{12x}{12} \\ 1.08 = x \end{array}$
Now It's Your Turn	<p>Solve each equation.</p> <p>a. $4(2x + 1) = 2(x - 13)$</p> $\begin{array}{r} 8x + 4 = 2x - 26 \\ -2x \quad -2x \\ \hline 6x + 4 = -26 \\ -4 \quad -4 \\ \hline 6x = -30 \\ \frac{6x}{6} = \frac{-30}{6} \\ x = -5 \end{array}$ <p>b. $7(4 - x) = 3(x - 4) + 5x$</p> $\begin{array}{r} 28 - 7x = 3x - 12 + 5x \\ 28 - 7x = 8x - 12 \\ +7x \quad +7x \\ \hline 28 = 15x - 12 \\ +12 \quad +12 \\ \hline 40 = 15x \\ \frac{40}{15} = \frac{15x}{15} \\ 2.7 = x \end{array}$

Example 2: Equations with Special Solutions

Solve each equation.

a. $10x + 12 = 2(5x + 6)$

$$\begin{array}{r} 10x + 12 = 10x + 12 \\ -10x \quad -10x \\ \hline 12 = 12 \\ \text{Always true} \end{array}$$

All real numbers

b. $9m - 4 = -3m + 5 + 12m$

$$\begin{array}{r} 9m - 4 = 9m + 5 \\ -9m \quad -9m \\ \hline -4 = 5 \\ \text{Never true} \end{array}$$

No solution

Now It's Your Turn

Solve each Equation.

a. $3(4b - 2) = -6 + 12b$

$$\begin{array}{r} 12b - 6 = -6 + 12b \\ -12b \quad -12b \\ \hline -6 = -6 \end{array}$$

All real numbers

b. $2x + 7 = -1(3 - 2x)$

$$\begin{array}{r} 2x + 7 = -3 + 2x \\ -2x \quad -2x \\ \hline 7 = -3 \end{array}$$

No solution

Equations with No Solutions

When the coefficients of x match (variables disappear) and the resulting statement is false

Equations with Infinitely Many Solutions

When the coefficients of x match (variables disappear) and the resulting statement is true.

Concept Summary: Solving Equations

Take note

Concept Summary Solving Equations

- Step 1** Use the Distributive Property to remove any grouping symbols. Use properties of equality to clear decimals and fractions.
- Step 2** Combine like terms on each side of the equation.
- Step 3** Use the properties of equality to get the variable terms on one side of the equation and the constants on the other.
- Step 4** Use the properties of equality to solve for the variable.
- Step 5** Check your solution in the original equation.

Summary: _____

Learning Target: Today you will be able to REWRITE LITERAL EQUATIONS

Question/Main Ideas:	Notes:
<p>Definition: Literal Equations</p>	<p>An equation that involves two or more variables.</p>
<p>Example 1: Rewriting a Literal Equation</p>	<p>Solve the given equation for y.</p> <p>a. $10x + 5y = 80$</p> $\begin{array}{r} -10x \quad -10x \\ \hline 5y = \frac{80-10x}{5} \end{array}$ $y = 16 - 2x$ <p>OR</p> $y = -2x + 16$ <p>b. $-2x + 5y = 12$</p> $\begin{array}{r} +2x \quad +2x \\ \hline 5y = \frac{12+2x}{5} \end{array}$ $y = \frac{12}{5} + \frac{2}{5}x$ <p>OR</p> $y = \frac{2}{5}x + \frac{12}{5}$
<p>Now It's Your Turn</p>	<p>Solve the given equation for y.</p> <p>a. $4 = 2y - 5x$</p> $\begin{array}{r} +5x \quad +5x \\ \hline 4 + 5x = 2y \end{array}$ $\frac{4+5x}{2} = \frac{2y}{2}$ $2 + \frac{5}{2}x = y$ <p>OR</p> $y = \frac{5}{2}x + 2$ <p>b. $x - 2y = -10$</p> $\begin{array}{r} -x \quad -x \\ \hline -2y = \frac{-10-x}{-2} \end{array}$ $y = 5 + \frac{1}{2}x$ <p>OR</p> $y = \frac{1}{2}x + 5$
<p>Example 2: Rewriting a Literal Equation with Only Variables</p>	<p>Solve $ax - by = c$ for x.</p> $\begin{array}{r} +by \quad +by \\ \hline ax = \frac{c+by}{a} \end{array}$ $x = \frac{c}{a} + \frac{by}{a}$ <p>OR</p> $x = \frac{c+by}{a}$

Now It's Your Turn

Solve $-x = r + py$ for y .

$$\frac{-x-r}{p} = \frac{py}{p} \quad y = \frac{-x-r}{p}$$

Definition: Formula

A special type of equation that shows the relationship between different variables.

Common Formulas

Formula Name	Formula	Definitions of Variables
Perimeter of a rectangle	$P = 2\ell + 2w$	P = perimeter, ℓ = length, w = width
Circumference of a circle	$C = 2\pi r$	C = circumference, r = radius
Area of a rectangle	$A = \ell w$	A = area, ℓ = length, w = width
Area of a triangle	$A = \frac{1}{2}bh$	A = area, b = base, h = height
Area of a circle	$A = \pi r^2$	A = area, r = radius
Distance traveled	$d = rt$	d = distance, r = rate, t = time
Temperature	$C = \frac{5}{9}(F - 32)$	C = degrees Celsius, F = degrees Fahrenheit

Example 3: Rewriting a Geometric Formula

Solve each equation for the given variable.

a. $C = \frac{2\pi r}{2\pi}$ for r

$$\frac{C}{2\pi} = r$$

b. $A = \frac{1}{2}bh$ for h

$$\frac{2A}{b} = \frac{bh}{b} \quad \frac{2A}{b} = h$$

Now It's Your Turn

Solve each equation for the given variable.

a. $D = \frac{rt}{r}$ for t

$$\frac{D}{r} = t$$

b. $C = \frac{5}{9}(F - 32)$ for F

$$\frac{9}{5}C = F - 32 \quad \frac{9}{5}C + 32 = F$$

Summary:

Learning Target: Today you will be able to SOLVE AND APPLY PROPORTIONS

Question/Main Ideas:	Notes:
<p>Definition: Proportion</p>	<p>An equation that states two ratios are equal.</p> $\frac{a}{b} = \frac{c}{d} \quad b \neq 0, d \neq 0$ <p>said "a is to b as c is to d"</p>
<p>Example 1: Solving a Proportion Using the Multiplication Property</p>	<p>Solve each equation.</p> <p>a. $\left(\frac{7}{8} = \frac{m}{12}\right) 96$</p> $\frac{84}{8} = \frac{8m}{8}$ $10.5 = m$ <p>b. Your Turn: $\left(\frac{x}{7} = \frac{4}{5}\right) 35$</p> $\frac{5x}{5} = \frac{28}{5}$ $x = 5.6$
<p>Property: Cross Products Property of a Proportion</p>	<p>The cross products of a proportion are equal.</p> <p>If $\frac{a}{b} = \frac{c}{d}$, then $ad = bc$</p> $\frac{3}{4} = \frac{9}{12} \quad 3 \cdot 12 = 4 \cdot 9$ $36 = 36$
<p>Example 2: Solving a Proportion Using the Cross Products Property</p>	<p>Solve each equation.</p> <p>a. $\frac{4}{3} = \frac{8}{x}$</p> $\frac{4x}{4} = \frac{24}{4}$ $x = 6$ <p>b. Your Turn: $\frac{x}{3} = \frac{3}{5}$</p> $\frac{5x}{5} = \frac{9}{5}$ $x = 1.8$

Example 3: Solving a Multi-Step Proportion

Solve each equation.

a. $\frac{x-8}{5} = \frac{x+3}{4}$

$$5(x+3) = 4(x-8)$$

$$5x + 15 = 4x - 32$$

$$\begin{array}{r} -4x \\ \hline \end{array}$$

$$x + 15 = -32$$

$$\begin{array}{r} -15 \\ \hline \end{array}$$

$$x = -47$$

b. Your Turn: $\frac{x}{5} = \frac{2x+4}{6}$

$$6x = 5(2x+4)$$

$$6x = 10x + 20$$

$$\begin{array}{r} -10x \\ \hline \end{array}$$

$$-4x = 20$$

$$\begin{array}{r} -4 \\ \hline \end{array}$$

$$x = -5$$

Example 4: Using a Proportion to Solve a Problem

A portable media player has 2 gigabytes of storage and can hold about 500 songs. A similar but larger media player has 80 gigabytes of storage. About how many songs can the larger media player hold?

$$\frac{\text{gb Large}}{\text{songs Large}} = \frac{\text{gb small}}{\text{songs small}}$$

$$\frac{80}{x} = \frac{2}{500}$$

$$\frac{2x}{2} = \frac{40000}{2}$$

$$x = 20,000 \text{ songs}$$

Now It's Your Turn

An 8-oz can of orange juice contains about 97 mg of vitamin C. About how many milligrams of vitamin C are there in a 12-oz can of orange juice?

$$\frac{\text{Large oz}}{\text{Large mg}} = \frac{\text{Small oz}}{\text{Small mg}}$$

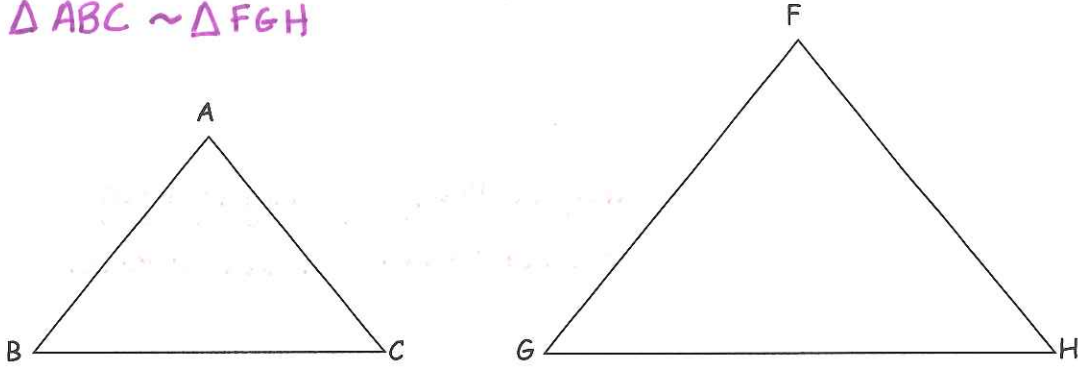
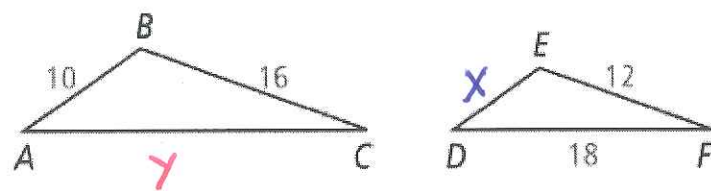
$$\frac{12}{x} = \frac{8}{97}$$

$$\frac{8x}{8} = \frac{1164}{8}$$

$$x = 145.5 \text{ mg}$$

Summary: _____

Learning Target: Today you will be able to SOLVE AND APPLY PROPORTIONS

Question/Main Ideas:	Notes:
<p>Definition: Similar Figures</p>	<p>Two figures that have the same shape, but not the same size. Angles are the same; sides are proportional. \sim is the symbol for similar. \cong is the symbol for congruent</p>
<p>Diagram: Similar Figures</p>	<p>$\triangle ABC \sim \triangle FGH$</p>  <p> $\angle A \cong \angle F$ $\angle B \cong \angle G$ $\angle C \cong \angle H$ </p> <p> $\frac{AB}{FG} = \frac{AC}{FH} = \frac{BC}{GH}$ </p>
<p>Example 1: Finding the Length of a Side</p>	<p>Find the length of DE.</p>  <p> $\frac{AB}{DE} = \frac{BC}{EF}$ $\frac{10}{x} = \frac{16}{12}$ $\frac{16x}{16} = \frac{120}{16}$ </p> <p>$x = 7.5$</p>
<p>Now It's Your Turn</p>	<p>Use the same diagram above to find the length of AC.</p> <p> $\frac{BC}{EF} = \frac{AC}{DF}$ $\frac{16}{12} = \frac{y}{18}$ $12y = 288$ $y = 24$ </p>

Example 2: Applying Similarity

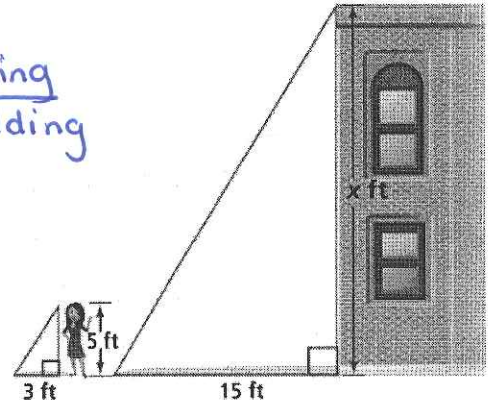
The sun's rays strike the building and the girl at the same angle, forming two similar triangles shown. How tall is the building?

$$\frac{\text{Height Girl}}{\text{Shadow Girl}} = \frac{\text{Height Building}}{\text{Shadow Building}}$$

$$\frac{5}{3} = \frac{x}{15}$$

$$3x = 75$$

$$x = 25 \text{ ft}$$



Now It's Your Turn

A man who is 6 ft tall is standing next to a flagpole. The shadow of the man is 3.5 ft and the shadow of the flagpole is 17.5 ft. What is the height of the flagpole?

$$\frac{\text{Height Man}}{\text{Shadow Man}} = \frac{\text{Height Pole}}{\text{Shadow Pole}}$$

$$\frac{6}{3.5} = \frac{x}{17.5} \quad x = 30 \text{ ft}$$

$$3.5x = 105$$

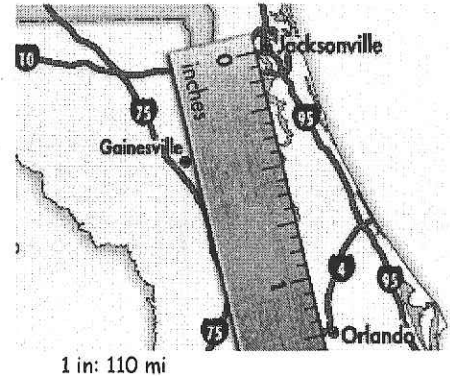
Example 3: Interpreting Scale Drawings

What is the actual distance from Jacksonville to Orlando? Use the ruler to measure the distance from Jacksonville to Orlando on the map.

$$\frac{\text{Scale in}}{\text{Scale mi}} = \frac{\text{Actual in}}{\text{Actual mi}}$$

$$\frac{1}{110} = \frac{1.25}{x}$$

$$x = 137.5 \text{ mi}$$



Now It's Your Turn

The distance from Jacksonville to Gainesville on the map is about 0.6 in. What is the actual distance from Jacksonville to Gainesville?

$$\frac{1}{110} = \frac{0.6}{x} \quad x = 66 \text{ mi}$$

Summary: _____
